

SOME REMARKS ON SUPERSTRING PHENOMENOLOGY*

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ABSTRACT

The present status of superstring phenomenology is briefly discussed.

1. Introduction

The number of consistent string models is huge and largely unexplored. One should probably consider these models as different classical vacua of a single theory, likely to be connected by some continuous parameters, or moduli; if so, progress to locate the correct vacuum that describes our universe will be extremely difficult, mainly due to our lack of understanding of the complete moduli space (or, the space of models), and its relevant underlying dynamics. Fortunately, we know quite a lot about our universe. Assuming that superstring does describe our universe, we may use the experimental data to guide the search of the string model that governs our world. This approach is known as superstring phenomenology.

It is reasonable to assume that nature has an underlying supersymmetry (SUSY), so we may start with a specific heterotic string model with $N = 1$ space-time supersymmetry. Of course this supersymmetry must be dynamically broken to reproduce the observed universe. *A priori*, dynamical SUSY breaking in string theory is very difficult to study, since it involves the strong coupling regime of string theory. Fortunately, the array of recent works ¹ on string-string duality offers a plausible resolution to this problem. String-string duality identifies the strong coupling limit of a heterotic string model with the weak coupling limit of a specific Type II string model. Since supersymmetry is broken, this Type II model must have no space-time supersymmetry, *i.e.*, it is an $N = 0$ model. A typical string model will have an observable sector, which contains the standard model, and a hidden sector (The need for a hidden sector was recognized even before the modern advance of the superstring theory ²). One then expects that dynamical supersymmetry breaking emerges from the strongly coupled hidden sector of the heterotic string model, while the observable

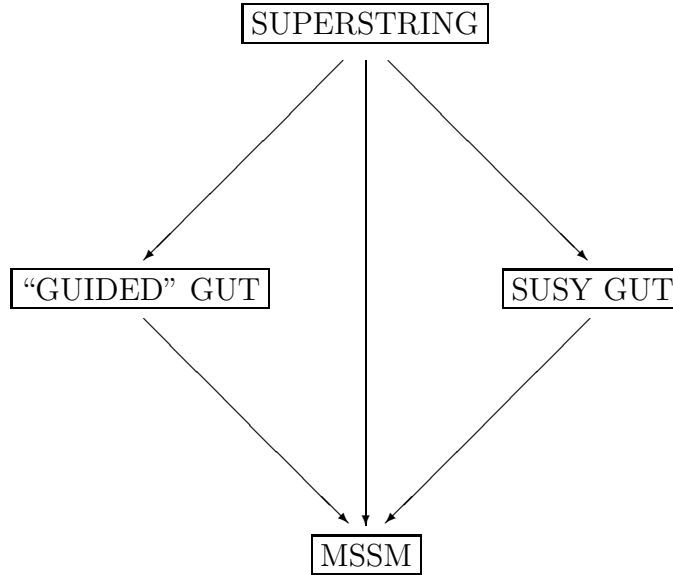
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sector remains weakly coupled. This suggests that the (semi-)classical description of the observable sector in the heterotic string model may be quite close to what is really happening in nature, while one can look at its Type II dual partner to study the supersymmetry breaking pattern. This justifies the search for string models whose visible sectors resemble nature. Such models should have hidden sectors that contain asymptotically free gauge groups that become strongly coupled at scales below the string scale, triggering SUSY breaking. Fortunately, this seems to happen naturally in many examples.

What is a phenomenologically interesting string model? Roughly speaking, we want an $N = 1$ heterotic string model that has, in the visible sector of its low energy effective (supergravity) field theory limit, one of the following three features:

- (i) It contains the SUSY standard $SU(3) \otimes SU(2) \otimes U(1)$ model. The simplest standard model is the minimal supersymmetric standard model (MSSM) ³. We shall generalize the definition of MSSM to allow the inclusion of additional superheavy particles. There are numerous examples of this type.
- (ii) It contains a SUSY grand unified theory (GUT). So far, the only examples of this type have four chiral families.
- (iii) It contains a so-called "guided" grand unified model. There are a number of examples of this type.

These possibilities are summarized in the following diagram:



Let us consider each of these cases in more detail.

2. Standard Model

Embedding the standard $SU(3) \otimes SU(2) \otimes U(1)$ model in string is relatively easy. There are many string models of this type in the literature ⁴.

There are a couple of issues that are worth mentioning here. At the string scale, the three gauge couplings of $SU(3) \otimes SU(2) \otimes U(1)$ must be equal. Now, the string scale M_{string} is

$$M_{\text{string}} = g M_{\text{Planck}} / 4\pi = 5 \times 10^{17} \text{ GeV} , \quad (0.1)$$

where g is the gauge coupling in a typical string model at the string scale. In MSSM, the three gauge couplings unify at around $3 \times 10^{16} \text{ GeV}$ ⁵, which is definitely below the string unification scale. Naively, this discrepancy is bothering. Fortunately, in many string models that have been looked at, this discrepancy is resolved by the presence of string thresholds⁶ and exotic matter fields⁷, which slightly modifies the running of the couplings in just the right amount so that the coupling unification moves from $3 \times 10^{16} \text{ GeV}$ to the string scale.

The total rank of the gauge groups in a generic heterotic string model in four space-time dimensions is 22 (for our counting purposes, a $U(1)$ has rank 1, and all solitons are massive) or less. If we choose the standard model as the gauge group for the visible sector, then the hidden (or semi-hidden) sector can have a gauge group whose rank can be as large as $22 - 4 = 18$. Such a large size allows for numerous possibilities. Since the hidden sector interacts with the observable sector only via the gravitational interaction, its impact on phenomenology is rather weak. Furthermore, since the hidden sector is expected to involve non-perturbative effects such as SUSY breaking, confrontation with phenomenological constraints entails large theoretical uncertainties. As a result, the possibilities of consistent choices for the hidden sector are myriad and largely unexplored; and it is not that difficult to find a string model that looks compatible with phenomenology, as testified by many such claims in the literature. The difficulty is the lack of an objective criteria that would select a particular model over all the others. Finding the dual partner of any of these models would go a long way in deciding its phenomenological viability, but this is not going to be easy.

3. Grand Unified Theories

Phenomenologically, grand unified theories (GUT) in the supergravity framework (with three chiral families, in particular) are rather appealing. These models have attracted a lot of attention. The LEP data on the unification of the couplings ⁵ added further motivation to this general idea. Recently, considerable effort has gone into the analysis of the fermion mass matrices in supersymmetric grand unified models. Generic features of these so called texture models ⁸ look very promising. Furthermore they suggest that it is natural and desirable, and may even be necessary, to embed such a framework in superstring.

So, how can we construct such a model? First, let us recall the following facts. It is well known that in field theory adjoint Higgs (or higher dimensional representations)

is necessary for a grand unified gauge group to break spontaneously to the $SU(3) \otimes SU(2) \otimes U(1)$ gauge group of the standard model. It is also known that, for Kac-Moody current algebras at level 1, space-time supersymmetry and chiral fermions cannot co-exist with massless scalar fields in the adjoint (or higher dimensional) representations of the gauge group in heterotic string models⁹. From these facts, we conclude that string GUT is possible only if the gauge group is realized via Kac-Moody current algebras at levels higher than 1. Phenomenologically, level-2 or -3 gauge groups look promising. Since higher-level current algebras have larger central charges, the construction of such gauge groups reduces the size of the hidden sector. This is an attractive feature because, with smaller rank size for the hidden sector, the number of possibilities is severely restricted.

The first higher level group in string theory appears in a ten-dimensional heterotic string model. In the classification of ten-dimensional models, all except one have rank 16 gauge groups (the best known ones are the supersymmetric $E_8 \otimes E_8$ and $SO(32)$ models). The exception is non-supersymmetric and tachyonic, with a (level-2) gauge group E_8 ¹⁰. Such uniqueness of higher level gauge groups in ten dimensions disappears in lower space-time dimensions. In four dimensions, in particular, there are models with higher level gauge groups and $N = 1$ space-time supersymmetry. Suppose we start from this (unique) single E_8 model. Since it is tachyonic, and so unstable, it must go to a stable string vacuum. (This is similar to spontaneous symmetry breaking when we start from a Higgs potential that, at zero vacuum expectation value, is tachyonic.) Starting from the point in the moduli space that describes this single E_8 model, it is possible that the nearby stable points all describe level-2 gauge groups. So models with level-2 gauge groups may be preferred.

The first string GUT was constructed by Lewellen¹¹. In particular, he constructed an $SO(10)$ string GUT with four chiral families. Next, Schwartz¹² constructed an $SU(5)$ string GUT, also with four chiral families. Both models are based on the free fermionic string construction¹³. *A priori*, there is nothing that prevents one from constructing a string GUT with three families. However, string GUT models are quite complicated. The construction of a typical higher-level string model involves a non-abelian asymmetric orbifold^{14,15}. The rules for model-building are easiest to use in the free fermionic string model construction; so it is not surprising that both of the known examples are constructed in this framework. However, the fermionic string construction involves multiple \mathbf{Z}_2 twists, and so the number of families naturally comes out in powers of 2. To obtain three families, we may use the so-called NAHE set¹⁶. This is achieved with the following observation. One can always cut the even number of families by half, in particular, one can cut two families to one, since $2^0 = 1$; in the case of level-1 groups there is plenty of room (i.e., $rank \text{ or } central \text{ charge} = 22$); so one can find three different sets (or sectors) of matter fields, each with a single family. As a result of this construction, these three families will have, beyond the standard $SU(3) \otimes SU(2) \otimes U(1)$ quantum numbers, different additional $U(1)$ charges.

Unfortunately, attempts to incorporate the NAHE set with a higher-level GUT gauge group have not been successful so far ¹⁷. This is probably because both the NAHE set and a higher-level gauge group need lots of space, which is not available within the free fermionic construction. Another promising possibility is have two families as a doublet, while the third heavy family is by itself ¹⁸. This way to incorporate three families will presumably take up less space than the NAHE set and is worth further investigation.

The above argument suggests that the free fermionic string model-building is not suitable for string GUTs with three families. But what if instead of a \mathbf{Z}_2 twist we try a \mathbf{Z}_3 twist, which typically yields families in powers of 3. However, various attempts along this direction has been unsuccessful so far. For example, using symmetric orbifolds, $SO(10)$ models with adjoint or 54 Higgs can be constructed ¹⁹, but they come with 4 families, not 3. Also an $SU(5)$ model with 3 families was constructed ¹⁹; unfortunately, the model also has exotic chiral families. Since higher-level gauge groups typically involve non-abelian orbifolds, one is led to consider asymmetric non-abelian orbifolds. Unfortunately, any realistic, or semi-realistic, model involves a somewhat complicated asymmetric non-abelian orbifold, and the rules for the construction of such models are not streamlined enough to allow a straightforward search. We believe this may be the reason that the search for string GUTs has stalled at this moment.

As optimists, we may consider the failure in the search so far as a good sign for string GUTs. In contrast to the standard model in string theory, where there is a proliferation of possibilities, the number of possible string GUTs should be very limited; it may even be unique. In view of this possibility, we feel further efforts in the search of string GUTs is worthwhile. As a first step, one should streamline the existing rules for model-building in string theory. Since the rules for the free fermionic string model construction are rather simple, we decide to extend these rules to include asymmetric ²⁰ and non-abelian orbifolds. In the following diagram the inside of the parallelogram schematically indicates the subspace of string models that can be obtained using free fermionic construction.

ORBIFOLD	SYMMETRIC	ASYMMETRIC
ABELIAN		
NON-ABELIAN		

In the near future, we intend to use the rules for asymmetric (non-)abelian model building to search for phenomenologically interesting string models as well as their

dual partners.

4. “Guided” GUTs

Let us now turn to the third possibility. As pointed out earlier, adjoint Higgs in a GUT comes only at the price of a higher-level construction. Actually, there is a way to have a grand unified gauge group without adjoint Higgs. This possibility appears quite naturally in string models. The first example of this type is the flipped $SU(5)$ model²². It turns out that this is a special case of a more general class of string models, which we shall refer to as “guided” GUTs. Let the GUT gauge group be G (typically $SU(5)$ or $SO(10)$). Then the gauge group of the guided GUT is $G \otimes G'$, where we shall call the group G' the “guiding” group. G' may be bigger, equal, or smaller than G . The basic idea of a “guided” GUT involves the presence of Higgs fields ϕ which are in non-trivial representations in both G and G' . When these Higgs fields develop appropriate vacuum expectation values that break $G \otimes G'$ to H , where $H \supseteq SU(3) \otimes SU(2) \otimes U(1)$, parts of H comes from both G and G' .

The Higgs fields employed in the “guided” GUTs are in representations lower than the adjoint representation. If $H = SU(3) \otimes SU(2) \otimes U(1)_Y$, further spontaneous symmetry breaking does not require adjoint Higgs. Since no adjoint Higgs are needed in these “guided” GUT models, level-1 gauge groups are perfectly adequate. Such gauge groups and their respective Higgs fields appear quite frequently in string models. To see if the Higgs fields do develop the appropriate vev, one has to study the Higgs potential. In many instances, the appropriate vev lies in a flat direction of the moduli space²¹, allowing for the particular vev choice demanded from phenomenology. In fact, this is a rather generic feature. The flipped $SU(5)$ string models have been studied in great detail²². The $SU(5)^3$ GUT as well as an $SO(10)^3$ GUT have been proposed²⁴. The $SU(5) \otimes SU(5)$ as well as the $SO(10)^3$ string models were recently constructed²⁵. For $G = SU(5)$, let us see how the Higgs mechanism works for the following choices, $G' = U(1)$, $SU(5)$, or $SU(5) \otimes SU(5)$; in each case, $H = SU(3) \otimes SU(2) \otimes U(1)_Y$. The basic idea of the $SO(10)$ case is very similar.

The simplest choice of $G' = U(1)$ yields the flipped $SU(5)$ model²³. It is instructive to start the discussion with $SO(10)$. Consider $SO(10) \supset SU(5) \otimes U(1)_X$, then the spinor representation of $SO(10)$ decomposes as $\mathbf{16} = \mathbf{10}(1) + \bar{\mathbf{5}}(-3) + \mathbf{1}(5)$, where the respective $U(1)_X$ charges X are given in brackets. Matter fields in the above combination will be anomaly-free. For $SU(5) \supset SU(3) \otimes SU(2) \otimes U(1)_Z$, we have

$$\begin{aligned}\mathbf{10} &= (\mathbf{1}, \mathbf{1})(1) + (\bar{\mathbf{3}}, \mathbf{1})(-2/3) + (\mathbf{3}, \mathbf{2})(1/6) , \\ \bar{\mathbf{5}} &= (\bar{\mathbf{3}}, \mathbf{1})(1/3) + (\mathbf{1}, \mathbf{2})(-1/2) , \\ \mathbf{1} &= (\mathbf{1}, \mathbf{1})(0) ,\end{aligned}$$

where the $U(1)_Z$ charges Z are also explicitly shown. Let us start from the guided GUT $SU(5) \otimes U(1)_X$ with three copies of chiral fermions given above. Suppose the

component $(1, 1)(1)(1)$ of a Higgs field $\mathbf{10}(1)$ develops a non-zero vacuum expectation value (vev). This field is singlet in $SU(3) \otimes SU(2)$ and neutral in $U(1)_Y$, where the hypercharge Y is a linear combination of the charges X and Z : $Y/2 = (X - Z)/5$. So the guided GUT spontaneously breaks to $SU(3) \otimes SU(2) \otimes U(1)_Y$, the standard model gauge group. In string theory, it is not hard to find a model with three chiral families and this Higgs field. The Higgs potential should develop a vev along the $(1, 1)(1)(1)$ direction. As a minimum requirement, the Higgs potential should be (perturbatively) flat along this direction. These flipped $SU(5)$ string models have been extensively studied. Since the rank of the gauge group of the hidden (plus semi-hidden) sector of such string models can be as large as 17, the choices is numerous.

In the case where $G' = SU(5)$, the desired Higgs fields are $\phi = (\mathbf{5}, \bar{\mathbf{5}})$ plus its complex conjugate. String models of this type have been constructed²⁵. The Higgs potential either develops a vev at, or has a flat direction along, $\langle \phi \rangle = \langle \phi^* \rangle = \text{diag}(X, X, X, -3X/2, -3X/2)$. With this vev, $SU(5) \otimes SU(5)$ spontaneously breaks to $SU(3) \otimes SU(2) \otimes U(1)_Y$.

For $G' = SU(5) \otimes SU(5)$, the Higgs fields are $(\mathbf{1}, \mathbf{5}, \bar{\mathbf{5}})$, $(\mathbf{5}, \bar{\mathbf{5}}, \mathbf{1})$ and $(\bar{\mathbf{5}}, \mathbf{1}, \mathbf{5})$ plus their complex conjugates. These three Higgs fields develop vevs of the form $\text{diag}(0, 0, 0, W, W)$, $\text{diag}(X, X, X, Z, Z)$ and $\text{diag}(U, U, U, 0, 0)$ respectively.

Although guided GUTs are rather ugly from the field theory point of view, they have a natural place in string models, due in part to the presence of flat directions in the Higgs potential. It is clearly worthwhile to explore these type of string models further. So far, only flipped $SU(5)$ has been investigated in any detail.

5. Summary

Starting with a specific heterotic string model, one derives its low energy effective (supergravity) field theory for energy scales below the string scale; this approach allows one to use field theoretic techniques to analyze many models and to impose phenomenological constraints. This is the old approach. With the recent understanding of string-string duality, one may be able to work directly in string theory. In fact, for non-supersymmetric models, we probably have a lot more control over its string version than over its field theory version. Hopefully, consistency of a dual pair of string models will impose tighter constraints on the selection of phenomenologically interesting string models.

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